



General information		Academic year 2022-2023
Academic subject	Introduction to the mathematical language	
Degree programme	Mathematics	
Programme year	First	
Term	First semester (September 12, 2022 – September 30, 2022)	
European Credit Transfer and Accumulation System credits (ECTS)	2	
Language	Italian	
Attendance	Compulsory	

Lecturers	
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Virtual meeting room	Microsoft Teams (see above)
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Office hours	Monday 14:30– 16:30 (presential or online meeting)

Syllabus	
Learning objectives	Completing prerequisites for the first-year university courses
Course prerequisites	High school mathematics
Course contents	<b>Logic and set theory</b> Logical connectives and truth tables. Conjunction, disjunction, negation. The implication: the principle of explosion ( <i>ex falso quodlibet</i> ), necessary condition and sufficient condition. The double implication or equivalence. Equivalent propositional forms. Negation of conjunctive and disjunctive propositional forms. Negation of an implication. Tautologies and contradictions. Universal and existential quantifier. Negation of universal and existential propositions. The form and the role of definitions. General form of the statement of a



theorem: hypothesis and conclusion. Examples of proofs and refutations, counterexamples. Direct and indirect proofs, *reductio ad absurdum*. The form and the role of characterizations.

Sets defined by properties. Set membership. Inclusion and equality by double inclusion. Strict inclusion. Distinct sets. Union, intersection, set difference. Complement sets. The empty set. Disjoint sets. Eulero-Venn diagrams. Proving some simple set-theoretical relations and properties. The well-ordering principle, the principle of induction and their applications to some arithmetical propositions. The relevance of the induction basis.

Cardinalities of finite sets. Infinite sets. The Cartesian product of sets. The cardinality of the Cartesian product of a finite family of finite sets. Permutations of  $n$  elements. The recursive formula for  $n!$ . Dispositions without repetitions and combinations of  $n$  elements  $k$  by  $k$ . The power set of a set and its cardinality in the finite case (proof of the formula by induction). Pascal's triangle. The combinatorial role of the binomial coefficients in Newton's binomial theorem. Binary arithmetic (a sketch).

#### **Mathematical analysis**

The real numbers. The algebraic and order axioms for real numbers. Dedekind's Axiom. Consequences of the axioms: uniqueness of zero, of the unity, of opposites, of reciprocals; zero-product property; sign properties of opposites and reciprocals; positivity of the unity. Representation of the real numbers on a line. Intervals and half-lines. The set  $\mathbf{N}$  of natural numbers and its properties. The set  $\mathbf{Z}$  of relative numbers and its properties. The set  $\mathbf{Q}$  of rational numbers and its properties.  $\mathbf{Q}$  does not fulfil Dedekind's Axiom. The incommensurability of the diagonal of the square with its side. Density of rational numbers in real numbers (without proof). Countable sets.  $\mathbf{N} \times \mathbf{N}$  is countable.  $\mathbf{Q}$  is countable.  $[0,1]$  is not countable. Representation of the real numbers by decimal expansion. Representation of the rational numbers by decimal expansion. An example of non-periodic decimal expansion. Approximation and rounding. Powers, monomials and polynomials with real coefficients. Operations on polynomials. Polynomial division. Roots of a polynomial and Ruffini's Rule. Polynomial factorization. Reminders on rational equations and inequations. The absolute value. Equations and inequations with absolute values. Irrational equations and inequations with one or two radicands. Elements of trigonometry. Trigonometric equations and inequations. Exponential and logarithmic equations and inequations.

#### **Geometry**

Relations between the elements of two sets. Binary relations on a set. Reflexive, symmetric, antisymmetric and transitive relations. Order and equivalence relations. Equivalence classes and their properties. Partitions. The quotient set as a partition. The equivalence relation determined by a partition.

Functional relations and functions; graph of a function. Fundamental examples: identity functions and constant functions. Direct image and inverse image of a subset; properties. Injective functions and their characterizations. Canonical injection. Surjective functions: definition and characterizations. Examples: the canonical surjection onto the quotient set. Bijective functions and their characterizations. The composition of functions and its properties. Invertible functions. Inverse functions. Characterization of invertible functions.

The Cartesian plane and its one-to-one correspondence with the set of

	ordered pairs of real numbers. Geometric loci and examples. Distance between two points and their midpoint. The Cartesian equation of a (straight) line; explicit equation of a line: geometric meaning of the slope. The Cartesian equation of the line through two given points. Parallel lines and their characterizations. Perpendicular lines and their characterizations. Generalities on conic sections and their equations. Elementary properties of binary operations: commutativity, associativity, distributivity, neutral element.
<b>Reference books</b>	Any textbook referring to the “precorso di matematica”
<b>Additional course materials</b>	Additional material will be uploaded to the Microsoft Teams platform and to the teachers’ homepages.

<b>Work schedule</b>				
	Total	Lectures	Hands-on learning (recitations/laboratories /seminars/other)	Self-study
<b>Hours</b>	50	50		
<b>ECTS credits</b>	2	2		

<b>Teaching methods</b>	
	Lectures

<b>Expected learning outcomes</b>	
<b>Knowledge and understanding</b>	Becoming familiar with the mathematical language
<b>Applying knowledge and understanding</b>	Translating mathematical statements from the verbal into the symbolic language, and conversely
<b>Making judgements</b>	Proving or disproving propositions
<b>Communication skills</b>	Expressing mathematical contents orally
<b>Learning skills</b>	Reading a mathematical text

<b>Assessment and feedback</b>	
Assessment methods	Final test (written, with multiple choice questions)
Evaluation criteria	<ul style="list-style-type: none"> <li>• <i>Knowledge and understanding</i>: Understanding the symbolic language</li> <li>• <i>Applying knowledge and understanding</i>: Explaining a mathematical content in one’s own words</li> <li>• <i>Making judgements</i>: Establishing the truth or falsity of a proposition</li> <li>• <i>Communication skills</i>: Presenting clear argumentations</li> <li>• <i>Learning skills</i>: Memorizing and reproducing statements</li> </ul>
Grading policy	Final test (written, with multiple choice questions)