

**Academic subject:** Mathematical Physics 1

<b>Degree Class:</b> L–35 – Scienze Matematiche	<b>Degree Course:</b> Mathematics	<b>Academic Year:</b> 2018/2019
	<b>Kind of class:</b> mandatory	<b>Year:</b> 2 <b>Period:</b> 2
		<b>ECTS:</b> 8 divided into <b>ECTS lessons:</b> 5 <b>ECTS</b> <b>exe/lab/tutor:</b> 3

**Time management, hours, in-class study hours, out-of-class study hours**

lesson: 40    exe/lab/tutor: 30    in-class study: 70    out-of-class study: 130

<b>Language:</b> Italian	<b>Compulsory Attendance:</b> no		
<b>Subject Teacher:</b> Lidia R. R. Palese	<b>Tel:</b> <b>e-mail:</b> lidiarosaria.palese@uniba.it	<b>Office:</b> Department of Mathematics Room 29, II Floor	<b>Office days and hours:</b> Wednesday 11-13. Other days and times by appointment.

**Prerequisites:**

Mathematical knowledge which usually is acquired during the first year of a degree of L–35 class, especially classical mathematical analysis of one and several variables, linear algebra.

**Educational objectives:**

Mathematical formulation, understanding and resolution of physical problems concerning the equilibrium of economic systems

<b>Expected learning outcomes (according to Dublin Descriptors)</b>	<p><b>Knowledge and understanding:</b> Acquiring fundamental concepts of the classical mechanics, , understanding physical, mathematical and geometrical aspects of a given problem</p> <p><b>Applying knowledge and understanding:</b> Ability to use theoretical knowledge in various statics problems.</p> <p><b>Making judgements:</b> Ability to identify mathematical tools and techniques to study physical problems written as mathematical models.</p> <p><b>Communication:</b> Students should acquire the mathematical language and formalism necessary to read and comprehend textbooks, to explain the acquired knowledge .</p> <p><b>Lifelong learning skills:</b> Acquiring suitable learning methods, supported by text consultation and by solving the questions periodically suggested during the course.</p>
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**Course program**

Elements of vector and matrix algebra: Vectors. Linear operators and their representations. Tensor product. Symmetric and antisymmetric operators. Unit operators, orthogonal and rotation operators. Projection operators. Eigenvalue problems. Positive definite operators.

Differential properties of the curves: the Frenet frame.

Applied vectors: Moment vectors with respect to a point or axis. Vector systems. Variation of the moment vector. Couple of applied vectors. Central axis of a vector system. Reduction of systems of applied vectors at a given point. Moments Transport Theorem. Systems whose parallel moment is null. Systems of parallel applied vectors.

Kinematics of a rigid body: The mathematical model of a rigid body. Body-fixed frames of reference. Angular velocity and Poisson formulas. The velocity field in a rigid body. Rigid motions and their classification. Euler angles. Lagrangian and Eulerian approach.. Eulerian velocity. Mozzi theorem.

Relative kinematics: Rate of change of a vector in a rotating frame. Velocity and acceleration addition theorems. Rolling of two surfaces.

Planar rigid motions: Center instantaneous of rotation. Analytical detection of the center.

Kinematics of holonomic systems: Constraints. Lagrangian coordinates and configuration space. Virtual and possible displacements. .Reversible and irreversible displacements.

Mass point geometry: The concepts of mass and density. Center of mass and its location. Inertia tensor. Eigenvalues and eigenvectors of the inertia tensor and their detection.. Huygens-Steiner theorem. Ellipsoid of inertia. Moment of inertia. The planar case. Linear and angular moments. Kinetic energy. Center of mass frame of reference. Konig theorems. Application to a rigid body and to a holonomic system. Work and potential: The concept of force. The work of a force. Conservative force. Work of a system of forces. Systems of conservative forces. Application to a rigid body and to an holonomic system. Classical mechanics principles: Friction. Constraints without friction. Principle of the constraint reactions. Pure rolling constraint. Statics of a point: static equilibrium and rest. Point constrained on a surface without friction. Point constrained on a curve without friction.

Principle of virtual works: a necessary and sufficient equilibrium condition. Application to a rigid free body, to a rigid

body with a fixed point, with a fixed axis or with a sliding axis on a fixed line.,, to an holonomic system. Statics equations: a necessary condition for the equilibrium. The case of a rigid body: the statics equations are necessary and sufficient for equilibrium. Applications of the statics equations to a rigid free body, to a rigid body with a fixed point, to a rigid body with a fixed axis, or with an axis sliding on a fixed line, to an holonomic system.

Dynamics of a material point: First integral, general and particular integrals. Kinetic energy theorem. The first integrals of the kinetic energy, of total mechanical energy.

Relative dynamics: Kinetic energy theorem. The two-body problem.

Equations of the motion: Dynamics of a system. General and particular integrals. Kinetic energy theorem. The first energy integral. Equation of mass center motion.

Lagrange equations: D'Alembert principle. Lagrange equations. Lagrange equations for potential forces.

Generalized potentials. General and particular integrals of the motion of an holonomic system. First integrals.

Cyclic coordinates.

#### **Teaching methods:**

Lectures and exercise sessions.

#### **Auxiliary teaching:**

Didactic material provided by the teacher

#### **Assessment methods:**

Oral exam.

#### **Bibliography:**

A. Strumia: MECCANICA RAZIONALE I, II. Edizioni Nautilus Bologna.

M. Fabrizio: Introduzione alla Meccanica Razionale e ai suoi metodi matematici. Zanichelli, 1997.