

Academic subject: Mathematical Physics 1			
Degree Class: L-35 – Scienze Matematiche		Degree Course: Mathematics	
		Academic Year: 2018/2019	
		Kind of class: mandatory	
		Year: 2	Period: 2
		ECTS:8 divided into ECTS lessons: 5 ECTS exe/lab/tutor: 3	
Time management, hours, in-class study hours, out-of-class study hours lesson: 40 exe/lab/tutor: 30 in-class study: 70 out-of-class study: 130			
Language: Italian		Compulsory Attendance: no	
Subject Teacher: Lidia R. R. Palese		Tel: e-mail: lidiarosaria.palese@uniba.it	
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		Office days and hours: Wednesday 11-13. Other days and times by appointment.	
Prerequisites: Mathematical knowledge which usually is acquired during the first year of a degree of L-35 class, especially classical mathematical analysis of one and several variables, linear algebra.			
Educational objectives: Mathematical formulation, understanding and resolution of physical problems concerning the equilibrium of olonomic systems			
Expected learning outcomes (according to Dublin Descriptors)		<p>Knowledge and understanding: Acquiring fundamental concepts of the classical mechanics, , understanding physical, mathematical and geometrical aspects of a given problem</p> <p>Applying knowledge and understanding: Ability to use theoretical knowledge in various statics problems.</p> <p>Making judgements: Ability to identify mathematical tools and techniques to study physical problems written as mathematical models.</p> <p>Communication: Students should acquire the mathematical language and formalism necessary to read and comprehend textbooks, to explain the acquired knowledge .</p> <p>Lifelong learning skills: Acquiring suitable learning methods, supported by text consultation and by solving the questions periodically suggested during the course.</p>	
<p>Course program</p> <p>Elements of vector and matrix algebra: Vectors. Linear operators and their representations. Tensor product. Symmetric and antisymmetric operators. Unit operators, orthogonal and rotation operators. Projection operators. Eigenvalue problems. Positive definite operators.</p> <p>Differential properties of the curves: the Frenet frame.</p> <p>Applied vectors: Moment vectors with respect to a point or axis. Vector systems. Variation of the moment vector. Couple of applied vectors. Central axis of a vector system. Reduction of systems of applied vectors at a given point. Moments Transport Theorem. Systems whose parallel moment is null. Systems of parallel applied vectors.</p> <p>Kinematics of a rigid body: The mathematical model of a rigid body. Body-fixed frames of reference. Angular velocity and Poisson formulas. The velocity field in a rigid body. Rigid motions and their classification. Euler angles. Lagrangian and Eulerian approach.. Eulerian velocity. Mozzi theorem.</p> <p>Relative kinematics: Rate of change of a vector in a rotating frame. Velocity and acceleration addition theorems. Rolling of two surfaces.</p> <p>Planar rigid motions: Center instantaneous of rotation. Analytical detection of the center.</p> <p>Kinematics of holonomic systems: Constraints. Lagrangian coordinates and configuration space. Virtual and possible displacements. .Reversible and irreversible displacements.</p>			

Mass point geometry: The concepts of mass and density. Center of mass and its location. Inertia tensor. Eigenvalues and eigenvectors of the inertia tensor and their detection.. Huygens-Steiner theorem. Ellipsoid of inertia. Moment of inertia. The planar case.
Linear and angular moments. Kinetic energy. Center of mass frame of reference. Konig theorems. Application to a rigid body and to a holonomic system.
Work and potential: The concept of force. The work of a force. Conservative force. Work of a system of forces. Systems of conservative forces. Application to a rigid body and to an holonomic system
Classical mechanics principles: Friction. Constraints without friction. Principle of the constraint reactions. Pure rolling constraint.
Statics of a point:static equilibrium and rest. Point constrained on a surface without friction. Point constrained on a curve without friction.

Principle of virtual works: a necessary and sufficient equilibrium condition. Application to a rigid free body, to a rigid

body with a fixed point, with a fixed axis or with a sliding axis on a fixed line., to an holonomic system.
Statics equations: a necessary condition for the equilibrium. The case of a rigid body: the statics equations are necessary and sufficient for equilibrium. Applications of the statics equations to a rigid free body, to a rigid body with a fixed point, to a rigid body with a fixed axis, or with an axis sliding on a fixed line, to an holonomic system.
Dynamics of a material point: First integral, general and particular integrals. Kinetic energy theorem. The first integrals of the kinetic energy, of total mechanical energy.
Relative dynamics: Kinetic energy theorem. The two-body problem .
Equations of the motion: Dynamics of a system. General and particular integrals . Kinetic energy theorem. The first energy integral. Equation of mass center motion..
Lagrange equations: D'Alembert principle. Lagrange equations . Lagrange equations for potential forces.
Generalized potentials. General and particular integrals of the motion of an holonomic system. First integrals.
Cyclic coordinates.

Teaching methods:

Lectures and exercise sessions.

Auxiliary teaching:

[Didactic material provided by the teacher](#)

Assessment methods:

Oral exam.

Bibliography:

- A. Strumia: MECCANICA RAZIONALE I, II. Edizioni Nautilus Bologna.
- M. Fabrizio: Introduzione alla Meccanica Razionale e ai suoi metodi matematici. Zanichelli, 1997.